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Howard Wainer: Graphic Discovery

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Why Playfair?

“Getting information from a table is like extracting sunbeams from a cucumber” (Farquhar and Farquhar).^{*} This evocative indictment of data tables by two nineteenth-century economists comes as no great insight to anyone who has ever tried to draw inferences from such a data display. For most purposes we almost always prefer a graphical representation. Indeed, graphs are ubiquitous now; hence it is hard to imagine a world before they existed. Yet data graphs are a human invention, indeed a relatively modern one. Data-based graphics began to make an appearance in the mid-seventeenth century but their full value and great popularity can be traced to a single event and a single person. The event was the publication, in 1786, of a small atlas describing the imports and exports of England and Wales with their various trading partners. The atlas contained forty-four graphs and no maps. Its author was a twenty-

seven-year-old Scot named William Playfair, and his *Commercial and Political Atlas* forever changed the way that we look at data.

William Playfair (1759–1823) worked as a draftsman for James Watt and was the ne’er-do-well younger brother of the well-known scientist John Playfair (1748–1814).[†] William Playfair is often credited with being the progenitor of modern statistical graphics. Most histories of statistical graphics give him huge credit while acknowledging important graphical work that preceded him.¹ A balanced summary is that he invented many of the currently popular graphical forms,[‡] improved the few that already existed, and broadly popularized the idea of graphic depiction of quantitative information. Before Playfair, statistical graphics were narrowly employed and even more narrowly circulated. After him, graphs popped up everywhere, being used to convey information in the social, physical, and natural sciences.

The title comes from Albert Biderman’s private characterization of the question that has intrigued him for more than a decade. The intellectual contents of this chapter come principally from two sources: Biderman’s 1978 talk at the Leesburg, Virginia, conference on Social Graphics (and its published elaboration, Biderman 1990) and Patricia Costigan-Eaves and Michael Macdonald-Ross’s extensive, but as yet unpublished, history of early graphic developments. Some of their material is in Costigan-Eaves and Macdonald-Ross 1990.

^{*} This well-known quotation, though pithy, is somewhat inaccurate. What the brothers Farquhar actually wrote (1891, p. 55) was, “The graphical method has considerable superiority for the exposition of statistical facts over the tabular. A heavy

bank of figures is grievously wearisome to the eye, and the popular mind is as incapable of drawing any useful lessons from it as of extracting sunbeams from cucumbers.”

[†] John Playfair’s activities were remarkably varied: minister, geologist, mathematician, and professor of natural philosophy at Edinburgh University. In fact, in 1805 William thanked his brother for the idea of using “lines applied to matters of finance” that William used in his 1786 book. We can only speculate why it took him nineteen years to give his brother some credit.

[‡] *Invented* is perhaps too strong a term. It may be more accurate to refer to him as an important deployer of graphical forms. He did not invent so much as he permuted and manip-

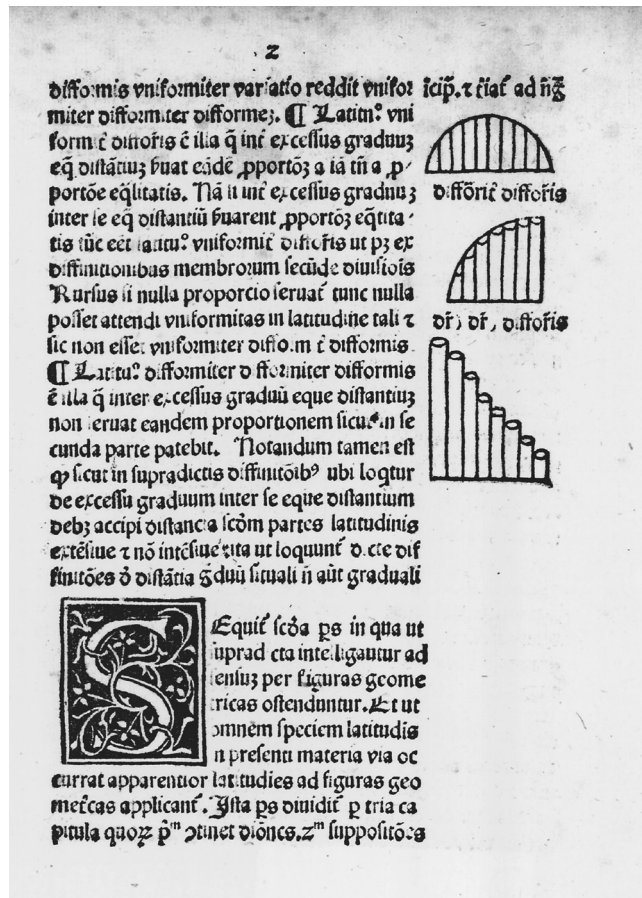


Figure 1.1. The first page of Oresme's *Tractatus de latitudinibus formarum*, the Padua edition of 1486. This item is reproduced by permission of the Huntington Library, San Marino, California.

Before we meet Playfair, however, it is worthwhile to step back a century or so and examine the attitudes that pervaded scientific investigations. Because natural science originated within natural philosophy, it favored a rational rather than an empirical approach to

ulated graphic elements; he varied graphic codes and formats as experiments to try to improve the visual portrayal of quantitative relationships. But there is no doubt that Playfair's use of graphics was more influential than his predecessors'. Part of this must have been because Playfair's graphs were so beautifully produced (compare his line charts with those of Huygens), but more important is the undeniable fact that Playfair published statistical graphics for all to see. Moreover, he did this repeatedly, and with a coherent theme, thus powerfully making the

scientific inquiry. Such an outlook was antithetical to the more empirical modern approach to science, which does not disdain the atheoretical plotting of data points with the goal of investigating suggestive patterns. Graphs that were in existence before Playfair (with some notable exceptions that I will discuss shortly) grew out of the same rationalist tradition that yielded Descartes's coordinate geometry—that is, the plotting of curves on the basis of an a priori mathematical expression. For example, Oresme's "pipes" on the first page of the Padua edition of his 1486 *Tractatus de latitudinibus formarum* (figure 1.1) is often cited as an early example.*

This notion is supported by statements such as that of Luke Howard, a prolific grapher of data in the late eighteenth and early nineteenth centuries who, as late as 1844, apologized for his methodology and referred to it as an "autograph of the curve . . . confessedly adapted rather to the use of the *dilettanti* in natural philosophy than that of regular students."

All the mechanical pieces necessary for data-based graphics were in place long before Playfair. For example, a primitive coordinate system of intersecting horizontal and vertical lines that enable a precise placement of data points was used by surveyors of the Nile flood basin as early as 1400 B.C. A more refined coordinate system was used by Hipparchus (ca. 140 B.C.), whose terms for the coordinate axes translate into Latin as *longitudo* and

point that the graphical depiction of information can communicate quantitative information in an accurate and relatively painless way.

* Clagett (1968) argued convincingly that this work was not written by Oresme, but probably by Jacobus de Sancto Martino, one of his followers, in about 1390—yet another instance of how surprisingly often eponymous referencing is an indication only of who did not do it (Stigler 1980).

latitudo, to locate points in the heavens. Somewhat later, Roman surveyors used a coordinate grid to lay out their towns on a plane that was defined by two axes. The *decimani* were lines running from east to west, and the *cardi* ran north to south.² Many other special-purpose coordinate systems were in wide use before Playfair: for example, musical notation placed on horizontal running lines was in use as early as the ninth century,³ and the chessboard was invented in seventh-century India.

One of the earliest examples of printed graph paper dates from about 1680.⁴ Large sheets of paper engraved with a grid were apparently printed to aid in designing and communicating the shapes of the hulls of ships.* Many historians describe Descartes's 1637 development of a coordinate system as an important intellectual milestone in the path toward statistical graphics.⁵ More recent work interprets this in exactly the opposite way—as an intellectual impediment that took a century and a half and Playfair's eclectic mind to overcome.⁶

Although the use of coordinate grids is very old, graphic encoding of information is older still. Paleolithic cave art provides an early and very striking example of graphic display. Some Ice Age bone carvings of animals are intermixed with patterns of dots and strokes that some archeologists have interpreted as a lunar notation system related to the animals' seasonal appearance. These are almost identical in structure, as well as degree of detail, to the engraving on the hull of the Pioneer 10 spacecraft that shows a drawing of a man and a woman along with a simple plotting of the Earth's location by dotted pulsar beams.

* This material is classed in the "collection" category of the British Library with the entry, "A collection of engraved sheets

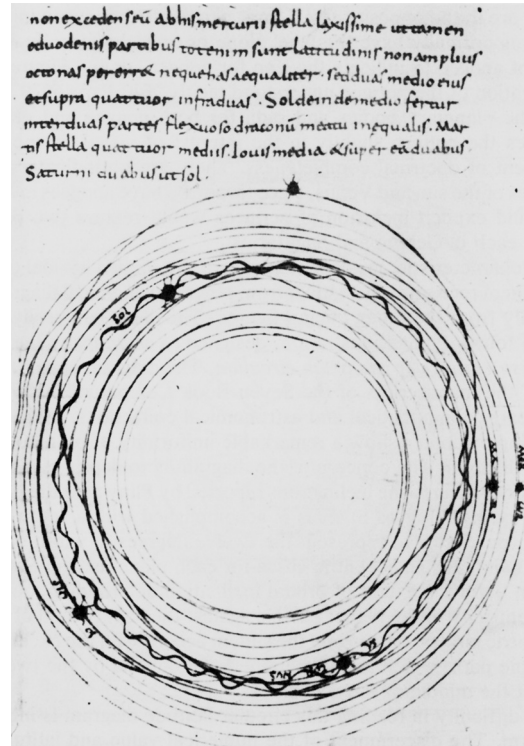


Figure 1.2. Plinian circular diagram of planetary latitudes, early ninth century. Taken from Eastwood (1987), p. 158, figure 6.

So we have the ideas of graphic encoding of information and a coordinate grid system. Why not the plotting of data? Well, some data were plotted. Let us consider three examples.

Example 1. Pliny's Ninth-Century Astronomical Charts

Pliny's (ca. 810) astronomical data were plotted in a roughly circular form (see figure 1.2) corresponding to the varying locations of the bodies in the heavens. But these graphs (astronomical maps) were not as useful as they might have been, because locating a body in the circular path required visually tracking the

of squared paper, whereon are traced in pencil or ink the curves or sweeps of the hulls of sundry men-of-war."

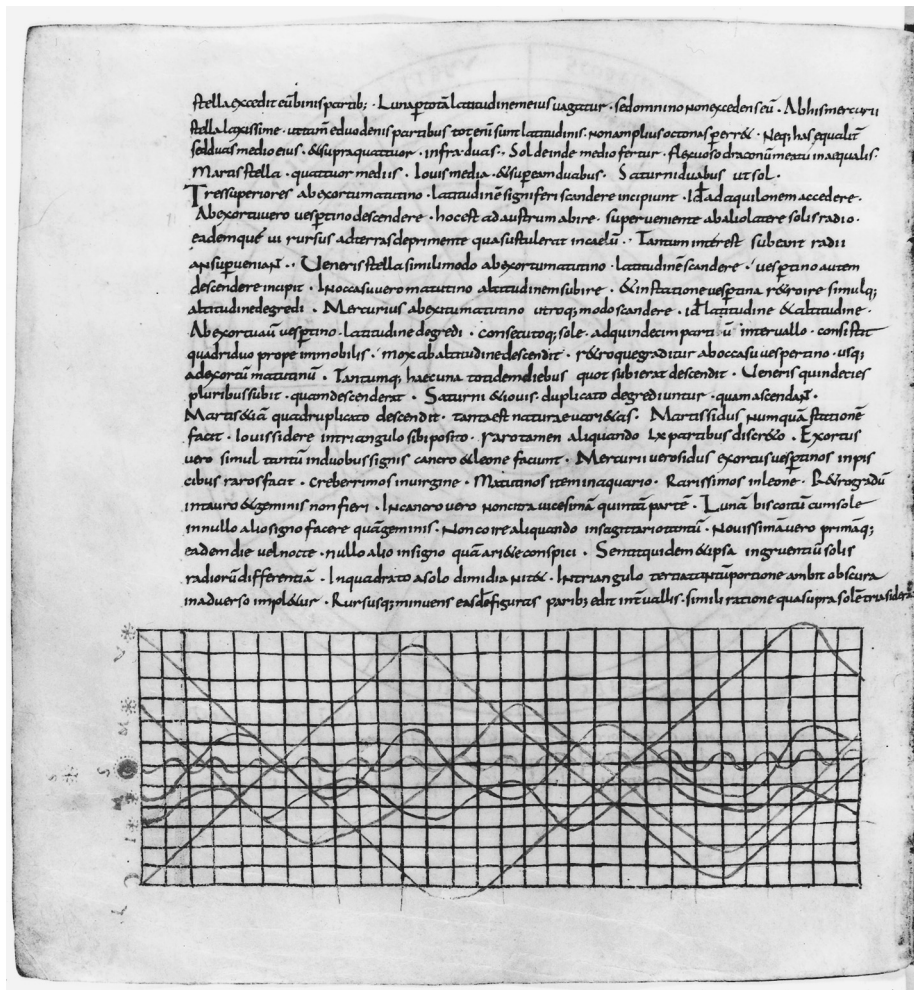


Figure 1.3. Plinian planetary latitudes, portrayed on a rectangular grid. Photo courtesy Burgerbibliothek Bern, ms. 367 f. 24v.

complete cycle. A manuscript originating in Auxerre toward the end of the ninth century contained a scheme that remedied this by transforming the circular grid into a rectangular one (see figure 1.3). The cyclic nature of the orbit is less apparent, but by making explicit the time (horizontal axis) and height above the horizon (vertical axis) it made locating and identifying a heavenly body somewhat easier.*

* There is actually less here than meets the eye. The horizontal axis is not particularly well defined. It is really an unfold-

Example 2. Christiaan Huygens's Seventeenth-Century Survival Charts

On October 30, 1669, the Dutch polymath Christiaan Huygens (1629–1693) received a letter from his brother Lodewijk containing some interpolations of life expectancy data taken from John Graunt's 1662 book *Natural and Political Observations on the Bills of Mortality*. Christiaan responded in letters

ing of the circular version with the horizontal spacing being only roughly related to time

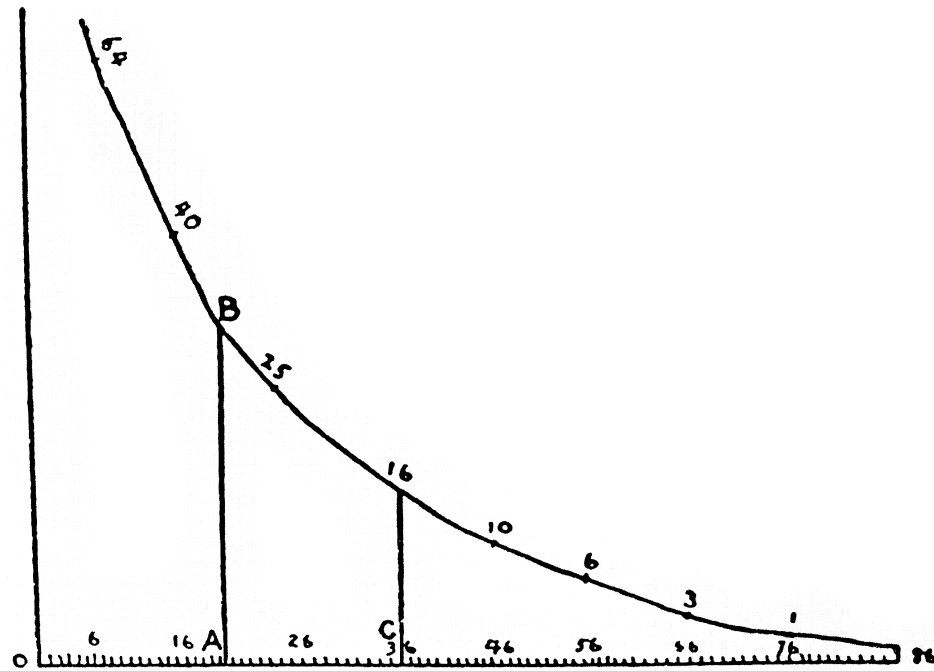


Figure 1.4. Christiaan Huygens's 1669 curve showing how many people out of a hundred survive between the ages of infancy and eighty-six. The data are taken from John Graunt, *Natural and Political Observations on the Bills of Mortality* (1662).

dated November 21 and 28, 1669, with graphs of those interpolations. Figure 1.4 contains one of those graphs showing age on the horizontal axis and number of survivors of the original birth cohort on the vertical axis. The curve drawn was fitted to his brother's interpolations.* The letters on the chart are related to an associated discussion on how to construct a life expectancy chart from this one—that is, analyzing a set of data to gain deeper insights into the subject. Christiaan con-

structed such a chart and indicated that it was more interesting from a scientific point of view; figure 1.4, he felt, was more helpful in wagering.†

Example 3. Robert Plot's Seventeenth-Century Plots of Barometric Pressure

Good graphs can make difficult problems trivial. We have all become used to weather forecasts that are very accurate and detailed for a

* Huygens's twenty-two-volume *Oeuvres complètes* (1888–1950) contains many other graphical devices to be explored by anyone with fluency in ancient Dutch, Latin, and French. Incidentally, Huygens's graphical work on the pendulum proved to him that a pendulum's oscillations would be isochronic regardless of its amplitude. This discovery led him to build the first clock based on this principle.

† This scooped a 1976 paper by the Chicago statistician Sandy Zabell, whose graphical analysis of the *Bills of Mortality* found inconsistencies, clerical errors, and a remarkable amount

of other information, “much of it unappreciated at the time of their publication” (Zabell 1976, p. 27). Zabell's point, though implicit in his paper, is important in this discussion. As we illustrated in one situation in the introduction to this book, this was strong evidence that graphic display was not widely available. For had they been seen, these errors, which could not be missed with any sort of competent display, would have been discovered and eliminated.

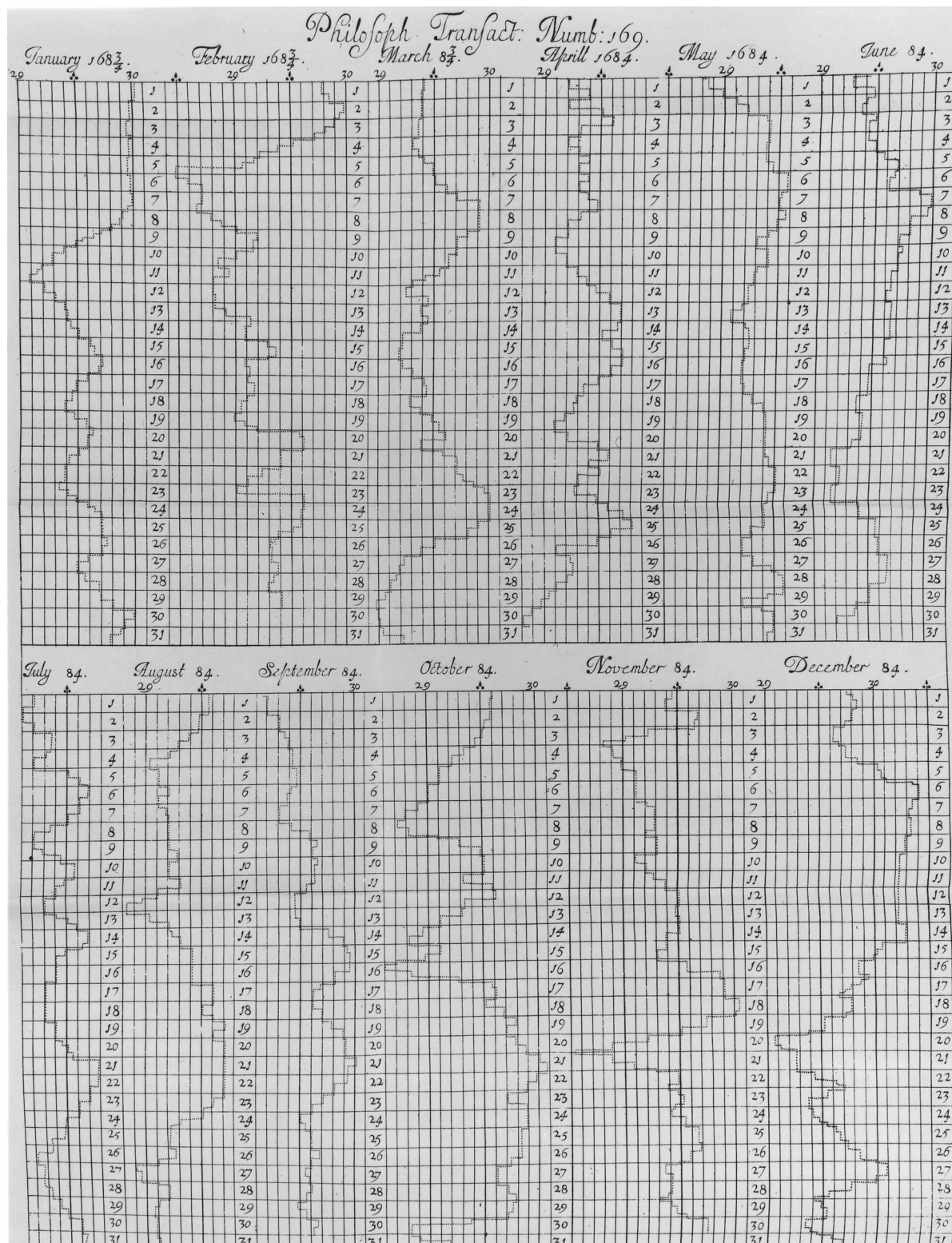


Figure 1.5. Robert Plot's (1685) "History of the Weather" recording of the daily barometric pressure in Oxford for the year 1684. Appears in *Philosophical Transactions* and is based on the original work of Martin Lister. Photo © The Royal Society.

day or two and pretty good for as far in advance as a week. I used to think that this was due to the increasing sophistication of complex prediction models.* But then I noticed the weather maps shown on every news broadcast. Using a model of no greater sophistication than that employed by Benjamin Franklin (weather generally moves from west to east), I was able to predict that the area of precipitation currently over Ohio would be hitting New Jersey by tomorrow and would stay over us until the weekend. Any fool could see it. The improvement in forecasting has not been entirely due to improvements in the mathematical models of the weather. The enormous wealth of radar and satellite data summarized into a multicolored and dynamic graphic can turn anyone into an expert.

The path to modern weather graphs is more than three hundred years long. The barometer was developed in 1665. Robert Plot recorded the barometric pressure in Oxford every day in 1684 and summarized his findings in a remarkably contemporary graph (figure 1.5) that he called a “History of the Weather.”

He sent a copy of this graph with a letter to Martin Lister† in 1685 with a prophetic insight:

For when once we have procured fit persons enough to make the same Observations in many foreign and remote parts, how the winds stood in each, at the same time, we shall then be enabled with some grounds to

examine, not only the coastings, breadth, and bounds of the winds themselves, but of the weather they bring with them; and probably in time thereby learn, to be forewarned certainly, of divers emergencies (such as heats, colds, dearths, plague, and other epidemical distempers) which are not unaccountable to us; and by their causes be instructed for prevention, or remedies: thence too in time we may hope to be informed how far the positions of the planets in relation to one another, and to the fixed stars, are concerned in the alterations of the weather, and in bringing and preventing diseases and other calamities . . . we shall certainly obtain more real and useful knowledge in matters in a few years, than we have yet arrived to, in many centuries.

WITH SO MANY PREDECESSORS, why have I chosen Playfair as my candidate for the father of modern graphical display? Although the arguments will build in subsequent chapters, a visual comparison of a sampling of Playfair’s plots with any of those that came before him makes clear the qualitative jump that Playfair’s work represents. Ian Spence points out that Playfair was the first to use hachure, color, and area to represent quantities in a systematic way. Moreover, Playfair published these forms in widely circulated volumes. Most of all, however, Playfair’s graphs provided proof that the presentation of evidence could be beautiful.

As but one such example, compare Playfair’s harmonious depiction of more than a century of data on England’s national debt

* It is true that models are more sophisticated than they were in the past. I was enormously impressed when some surprising turns in a hurricane’s path were predicted well in advance, but such models seem to be needed no more often than seldom.

† The origin of the graphical depiction of weather data, sadly, for the obvious eponymous glory, rests not with Plot but rather with Lister, who presented various versions of graphical

summaries of weather data before the Oxford Philosophical Society on March 10, 1683, and later in the same year presented a modified version to the Royal Society. Plot was not the only one enthusiastic about Lister’s graphical methods. William Molyneux was so taken that he had an engraving made of the grid, and he faithfully sent a “Weather Diary” monthly to William Musgrave. One of Molyneux’s charts was reproduced in Gunther (1968).

(figure 1.6) with any of the graphs produced previously by others. The viewer's eye is drawn from the soaring debt to the vertical lines that communicate the events that presaged a change in the debt. The viewer's mind cannot avoid making the causal inference suggested. Nothing that had been produced before was even close. Even today, after more than two centuries of graphical experience, Playfair's graphs remain exemplary standards for clear communication of quantitative phenomena.

It now seems wise to recapitulate the argument: Graphical forms were available before Playfair, but they were rarely used to plot empirical information. I argue that this was because there was an antipathy toward the empirical approach. This suggestion is supported by statements such as that made by Luke Howard. But at least sometimes when data were available (for example, Pliny's astronomical data, Graunt's survival data, Plot's weather data, and several other admirable uses), they were plotted. Could it be that the exponential increase in the use of graphics after the publication of Playfair's *Atlas* was merely concomitant to the exponential growth in the availability of data? Or did the availability of graphic devices for analyzing data encourage data gathering? And why Playfair? Was he merely at the cusp of an explosion in data gathering and so his graphic efforts appear causal? Or did he play an important role in that explosion?

The consensus of scholars is that until Playfair "many of the graphic devices used were the result of a formal and highly deductive science. . . . This world view was more comfortable with an arm-chair, rationalistic approach to problem-solving which usually

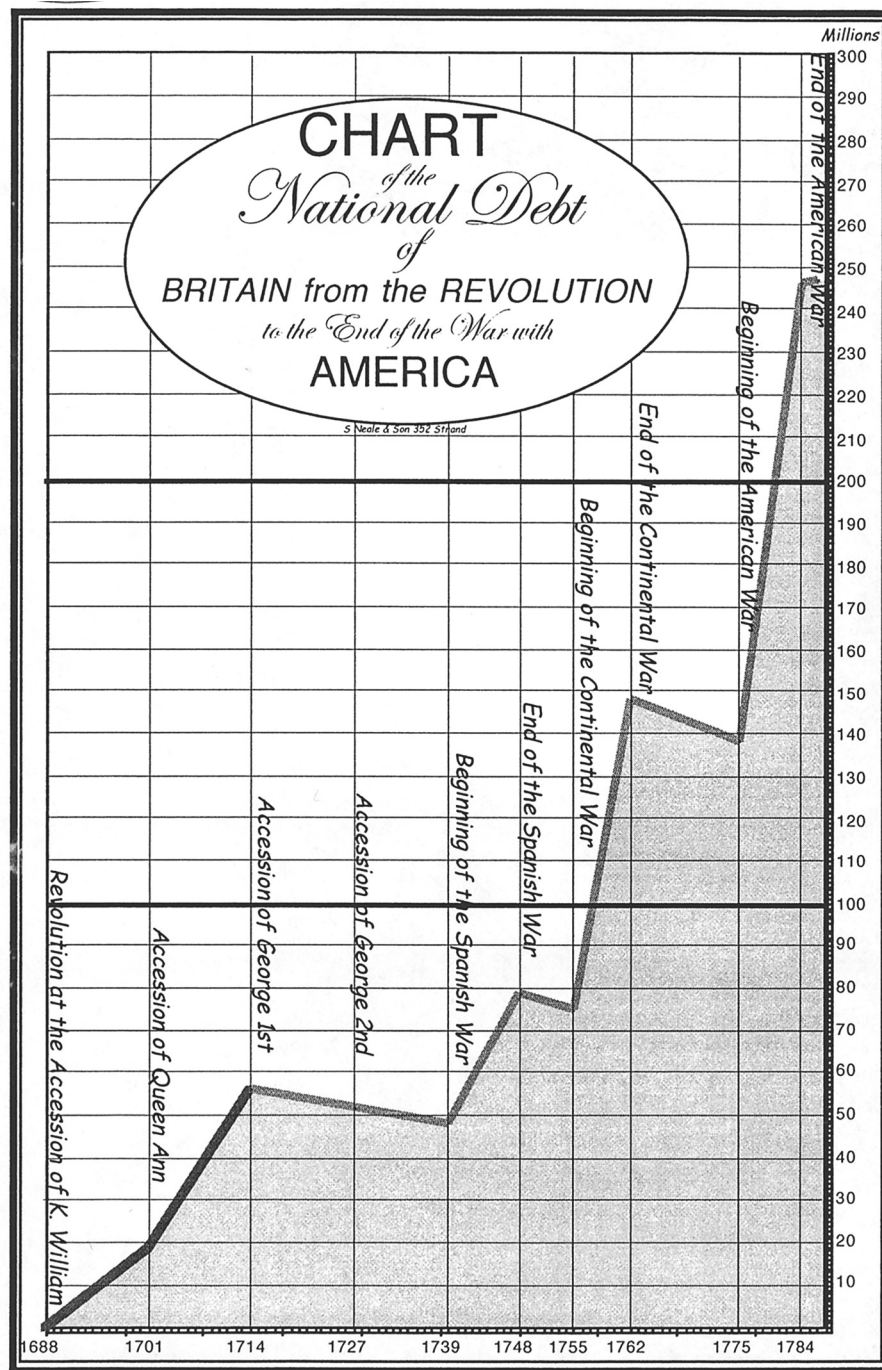
culminated in elegant mathematical principles" often associated with elegant geometrical diagrams.⁷ The empirical approach to problem solving, a critical driving force for data collection, was slow to emerge. But the empirical approach began to demonstrate remarkable success in solving problems, and with improved communications,* the news of these successes and hence the popularity of the associated graphic tools began to spread quickly.

So the picture is almost complete. The fundamental tools for the graphical display of data were available; there was an increase in the acceptance of an empirical approach to science as an important part of the scientific process; data were being gathered in greater and greater quantities; and the success of empirical procedures in solving important practical problems was being more widely communicated. This explains the growth of the graphical method, but still leaves the initial question, "Why Playfair?"

We are accustomed to intellectual diffusion taking place from the natural and physical sciences into the social sciences; certainly that is the direction taken for both calculus and the scientific method. But statistical graphics in particular, and statistics in general, went the reverse route. Although, as we have seen, there were applications of data-based graphics in the natural sciences, only after Playfair applied them in the social sciences did their popularity begin to accelerate. Playfair should be credited with producing the first chartbook of social statistics; indeed, publishing an *Atlas* that contained not a single map is one indication of his belief in the methodology (to say nothing of hischutzpah). Playfair's work was immediately admired, but emulation, at least

* The first encyclopedia in English appeared in 1704. The number of scientific periodicals began a rapid expansion at the end of the eighteenth century; between 1780 and 1789 twenty

new journals appeared, and between 1790 and 1800 twenty-five more (McKie 1972)



The Divisions at the Bottom are Years. & those on the Right hand Money

Figure 1.6. A close facsimile of William Playfair's plot of England's national debt from 1688 until 1786. It appeared in his *Commercial and Political Atlas* and accompanied his discussion arguing against the British government's policy of financing its colonial wars through debt.

in Britain, took a little longer (graphics use started on the continent a bit sooner). Interestingly, one of Playfair's earliest emulators was the banker S. Tertius Galton (the father of Francis Galton, and hence the biological grandfather of modern statistics), who in 1813 published a multiline time-series chart of the money in circulation, rates of foreign exchange, and prices of bullion and of wheat.* The relatively slower diffusion of the graphical method back into the natural sciences provides additional support for the hypothesized bias against empiricism there. The newer social sciences, having no such tradition and faced with both problems to solve and relevant data, were quicker to see the potential of Playfair's methods.

Playfair's graphical inventions and adaptations look contemporary. He invented the statistical bar chart out of desperation, because he lacked the time-series data required to draw a line showing the trade with Scotland and so

used bars to symbolize the cross-sectional character of the data he did have. Playfair acknowledged Priestley's priority in this form, although Priestley used bars to symbolize the life spans of historical figures in a time line.⁸ (See chapters 5, 6, and 7 for more on the fascinating history of time lines and graphical display of historical data.)†

Playfair's role was crucial for several reasons, but it was not for his development of the graphical recording of data; others preceded him in that. Indeed, in 1805 he pointed out that as a child his brother John had him keep a graphical record of temperature readings. But Playfair was in a remarkable position. Because of his close relationship with his brother and his connections with James Watt, he was on the periphery of science. He was close enough to know of the value of the graphical method, but sufficiently detached in his own interests to apply them in a very different arena—that of economics and finance.

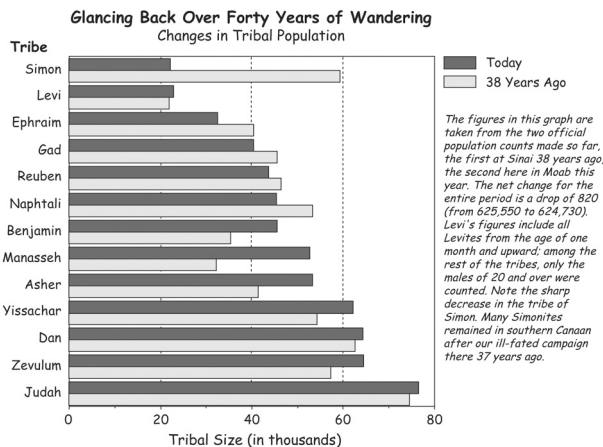


Figure 1.7. A translated and computer-enhanced reproduction of perhaps the earliest statistical graphic yet uncovered. It was apparently constructed about 1400 B.C. and was preserved in a sealed ceramic container in the Qumran caves. It was purchased by the author from Moishe the mapman at his Dead Sea antiquities stall in 1991.

* Biderman (1978) pointed out that, ironically, Galton's chart predicted the financial crisis of 1831 that created a ruinous run on his own bank.

† Priestley's use of the bar as a metaphor is somewhat different than Playfair's in that the data were not really statistical. A much earlier precedent has been recovered from its resting place in the Qumran caves abutting the Dead Sea. The graphic dates from approximately 1400 B.C. and was prepared as a summary of population changes in the twelve tribes of Israel as they emerged from their almost four decades of wandering in the Sinai after their exodus from Egypt, which began in April 1446 B.C. A faithful copy of this bar chart, with the captions and legends translated from Aramaic, is reproduced here as figure 1.7. Some aspects of this historic figure have been computer-enhanced for better reproduction. Note that it presages Huygens in subject matter and Playfair in form.

These areas, then as now, tend to attract a larger audience than matters of science, and Playfair was adept at self-promotion.

In a review of his 1786 *Atlas* that appeared in the *Political Herald*, Dr. Gilbert Stuart wrote,

The new method in which accounts are stated in this work, has attracted very general notice. The propriety and expediency of all men, who have any interest in the nation, being acquainted with the general outlines, and the great facts relating to our commerce are unquestionable; and this is the most commodious, as well as accurate mode of effecting this object, that has hitherto been thought of. . . . To each of his charts the author has added observations [that] . . . in general are just and shrewd; and sometimes profound. . . . Very considerable applause is certainly due to this invention; as a new, distinct, and easy mode of conveying information to statesmen and merchants.

Such wholehearted approval rarely greets any scientific development. Playfair's adaptation of graphic methods to matters of general interest provided an enormous boost to the popularity of statistical graphics. His energy and artistic sense showed themselves in the forty color charts in his initial *Atlas*. The size

of the undertaking required to produce such a book indicates Playfair's deep understanding of the power of the graphical method. His energy and skill as a draftsman, coupled with that understanding, led him to communicate his enthusiasm both widely and effectively. However, to be able to focus on graphics when the prevailing view of science looked upon such an approach as generally illegitimate requires a willingness to go against the tide—indeed, perhaps even taking joy in being an iconoclast. The events described in the next two chapters illuminate this aspect of Playfair's personality.

In *Kagemusha*, a film by the great Japanese director Akira Kurosawa, a legendary warlord is mortally wounded. The warlord's staff finds a petty thief, who bears a remarkable physical resemblance to the fallen leader, to substitute for him. With the substitute in place, the political strategy evolved by the dead warlord succeeds in his absence. In this examination of the question "the man or the moment?" Kurosawa clearly favors the latter. The Playfair enigma represents another instance of this great theme, although unlike Kurosawa's fictional situation, the more limited information available to us does not allow unambiguous conclusions.