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978-1-107-61967-8 - Large-Scale Inference: Empirical Bayes Methods for Estimation, Testing, and Prediction

Bradley Efron

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