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978-0-521-62116-8 - Fourier Analysis and Partial Differential Equations

Rafael Jose Iorio and Valeria de Magalhaes Iorio

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