

[A State Space Approach to Canonical Factorization with Applications](#)

Applications and Functions with Symmetry

Bearbeitet von
Harm Bart, Israel Gohberg, Marinus A. Kaashoek, André C.M. Ran

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Contents

Preface	xi
0 Introduction	1
Part I	
Convolution equations, canonical factorization and the state space method	7
1 The role of canonical factorization in solving convolution equations	9
1.1 Wiener-Hopf integral equations and factorization	9
1.2 Block Toeplitz equations and factorization	13
1.3 Singular integral equations and factorization	15
Notes	17
2 The state space method and factorization	19
2.1 Preliminaries on realization	19
2.2 Realization of rational matrix functions	22
2.3 Realization of analytic operator functions	23
2.4 Inversion	26
2.5 Products	27
2.6 Factorization	30
Notes	33
Part II	
Convolution equations with rational matrix symbols	35
3 Explicit solutions using realizations	37
3.1 Canonical factorization of rational matrix functions in state space form	37
3.2 Wiener-Hopf integral operators	42
3.3 Block Toeplitz operators	46
3.4 Singular integral equations	50
3.5 The Riemann-Hilbert boundary value problem	51
Notes	56

4	Factorization of non-proper rational matrix functions	57
4.1	Preliminaries about matrix pencils	57
4.2	Realization of a non-proper rational matrix function	59
4.3	Explicit canonical factorization	61
4.4	Inversion of singular operators with a rational matrix symbol	68
4.5	The Riemann-Hilbert boundary value problem revisited (1)	71
	Notes	74
 Part III		
	Equations with non-rational symbols	75
5	Factorization of matrix functions analytic in a strip	77
5.1	Exponentially dichotomous operators and bisemigroups	78
5.2	Spectral splitting and proof of Theorem 5.2	81
5.3	Realization triples	87
5.4	Construction of realization triples	91
5.5	Inverting matrix functions analytic in a strip	93
5.6	Inverting full line convolution operators	98
5.7	Inverting Wiener-Hopf integral operators	100
5.8	Explicit canonical factorization	106
5.9	The Riemann-Hilbert boundary value problem revisited (2)	111
	Notes	113
6	Convolution equations and the transport equation	115
6.1	The transport equation	116
6.2	The case of a finite number of scattering directions	118
6.3	Wiener-Hopf equations with operator-valued kernel functions	122
6.4	Construction of a canonical factorization	124
6.5	The matching of the subspaces	135
6.6	Formulas for solutions	138
	Notes	142
7	Wiener-Hopf factorization and factorization indices	143
7.1	Canonical factorization of operator functions	143
7.2	Proof of Theorem 7.2	147
7.3	Wiener-Hopf factorization and spectral invariants	157
	Notes	167

Part IV	
Factorization of selfadjoint rational matrix functions	169
8 Preliminaries concerning minimal factorization	171
8.1 Minimal realizations	171
8.2 Minimal factorization	174
8.3 Pseudo-canonical factorization	176
Notes	178
9 Factorization of positive definite rational matrix functions	181
9.1 Preliminaries on selfadjoint rational matrix functions	181
9.2 Spectral factorization	185
9.3 Positive definite functions on the unit circle	189
Notes	195
10 Pseudo-spectral factorizations of selfadjoint rational matrix functions	197
10.1 Nonnegative rational matrix functions	197
10.2 Selfadjoint rational matrix functions and further generalizations . .	205
Notes	209
11 Review of the theory of matrices in indefinite inner product spaces	211
11.1 Subspaces of indefinite inner product spaces	211
11.2 H -selfadjoint matrices	212
11.3 H -dissipative matrices	215
Notes	216
Part V	
Riccati equations and factorization	217
12 Canonical factorization and Riccati equations	219
12.1 Preliminaries on spectral angular subspaces	219
12.2 Angular operators and factorization	221
12.3 Riccati equations and canonical factorization	227
12.4 Left versus right canonical factorization	229
Notes	231
13 The symmetric algebraic Riccati equation	233
13.1 Spectral factorization and Riccati equations	233
13.2 Stabilizing solutions	238
13.3 Symmetric Riccati equations and pseudo-spectral factorization . .	242
Notes	247

14 J-spectral factorization	249
14.1 Definition of J -spectral factorization	249
14.2 J -spectral factorizations and invariant subspaces	251
14.3 J -spectral factorizations and Riccati equations	256
14.4 Two special cases of J -spectral factorization	259
14.5 J -spectral factorization with respect to other contours	262
14.6 Left versus right J -spectral factorization	273
14.7 J -spectral factorization relative to the unit circle revisited	276
Notes	288
 Part VI	
Factorizations and symmetries	289
 15 Factorization of positive real rational matrix functions	291
15.1 Rational matrix functions with a positive definite real part	291
15.2 Canonical factorization of functions with a positive definite real part	294
15.3 Generalization to pseudo-canonical factorization	297
Notes	300
 16 Contractive rational matrix functions	301
16.1 State space analysis of contractive rational matrix functions	301
16.2 Strictly contractive rational matrix functions	304
16.3 An application to spectral factorization	305
16.4 An application to canonical factorization	307
16.5 A generalization to pseudo-canonical factorization	309
Notes	312
 17 J-unitary rational matrix functions	313
17.1 Realizations of J -unitary rational matrix functions	313
17.2 Factorization of J -unitary rational matrix functions	321
17.3 Factorization of unitary rational matrix functions	324
17.4 Intermezzo on the Redheffer transformation	328
17.5 J -inner rational matrix functions	333
17.6 Inner-outer factorization	336
17.7 Unitary completions of minimal degree	339
17.8 Bi-inner completions of inner functions	341
Notes	345

Part VII	
Applications of J-spectral factorizations	347
18 Application to the rational Nehari problem	349
18.1 Problem statement and main result	349
18.2 Intermezzo about linear fractional maps	352
18.3 The J -spectral factorization approach	359
18.4 Proof of the main result	361
18.5 The case of a non-stable given function	366
18.6 The Nehari-Takagi problem	368
Notes	370
19 Review of some control theory for linear systems	371
19.1 Stability and feedback	371
19.2 Parametrization of internally stabilizing compensators	374
Notes	378
20 H-infinity control applications	379
20.1 The standard problem and model matching	380
20.2 The one-sided model matching problem	382
20.3 The two-sided model matching problem	386
20.4 State space solution of the standard problem	392
Notes	404
Bibliography	405
List of symbols	415
Index	419