

Elements of Numerical Relativity and Relativistic Hydrodynamics

From Einstein' s Equations to Astrophysical Simulations

Bearbeitet von
Carles Bona, Carlos Palenzuela-Luque, Carles Bona-Casas

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