

[Homological Algebra of Semimodules and Semicontramodules](#)

Semi-infinite Homological Algebra of Associative Algebraic Structures

Bearbeitet von
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