

Disorder and Critical Phenomena Through Basic Probability Models

École d'Été de Probabilités de Saint-Flour XL – 2010

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